

Ontologies - Querying Data through Ontologies

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Outline

- 1 Introduction
 - The Semantic Web
 - Ontologies and Reasoning
 - Illustration
- 2 3 ontology languages for the Web
- 3 Reasoning in Description Logics
- 4 Querying Data through Ontologies
- 5 Conclusion

The Semantic Web

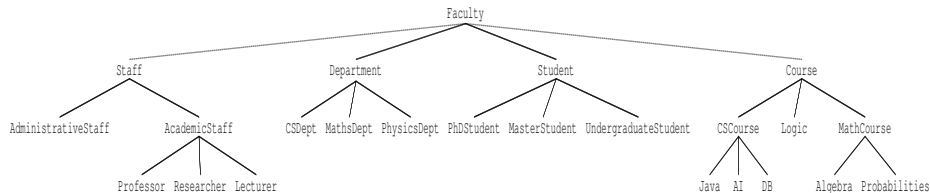
- A Web in which the resources are **semantically** described
 - ▶ annotations give information about a page, explain an expression in a page, etc.
- More precisely, a resource is anything that can be referred to by a **URI**
 - ▶ a web page, identified by a URL
 - ▶ a fragment of an XML document, identified by an element node of the document,
 - ▶ a web service,
 - ▶ a thing, an object, a concept, a property, etc.
- Semantic annotations: logical assertions that relate resources to some terms in pre-defined **ontologies**

Ontologies

- Formal descriptions providing **human** users a shared understanding of a given domain
 - ▶ A controlled vocabulary
- Formally defined so that it can also be processed by **machines**
- **Logical semantics** that enables **reasoning**.
- Reasoning is the key for different important tasks of Web data management, in particular
 - ▶ to answer queries (over possibly distributed data)
 - ▶ to relate objects in different data sources enabling their integration
 - ▶ to detect inconsistencies or redundancies
 - ▶ to refine queries with too many answers, or to relax queries with no answer

Classes and class hierarchy

- Backbone of the ontology
- AcademicStaff is a **Class**
- (A class will be interpreted as a **set** of objects)
- AcademicStaff **isa** Staff
- (isa is interpreted as set inclusion)



Relations

- Declaration of **relations** with their **signature**
- (Relations will be interpreted as binary relations between objects)
- `TeachesIn(AcademicStaff, Course)`
 - ▶ if one states that “`X TeachesIn Y`”, then `X` belongs to `AcademicStaff` and `Y` to `Course`,
- `TeachesTo(AcademicStaff, Student)`,
- `Leads(Staff, Department)`

Instances

- Classes have **instances**
- Dupond is an instance of the class `Professor`
- it corresponds to the fact: `Professor(Dupond)`

- Relations also have **instances**
- `(Dupond,CS101)` is an instance of the relation `TeachesIn`
- it corresponds to the fact: `TeachesIn(Dupond,CS101)`

- The instance statements can be seen as (and stored in) a **database**

Ontology = schema + instance

- **Schema**

- ▶ The set of class and relation names
- ▶ The **signatures** of relations and also **constraints**
- ▶ The constraints that are used for two purposes
 - ★ checking data consistency (like dependencies in databases)
 - ★ inferring new facts

- **Instance**

- ▶ The set of facts
- ▶ The set of base facts together with the inferred facts should satisfy the constraints

- **Ontology** (i.e., **Knowledge Base**) = Schema + Instance

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3 ontology languages for the Web

- RDF: a very simple ontology language
 - RDFS: Schema for RDF
 - ▶ Can be used to define richer ontologies
 - OWL: a much richer ontology language
-
- We next present them rapidly
 - We will introduce further a family of ontology languages: Description logics

RDF: Resource Description Framework

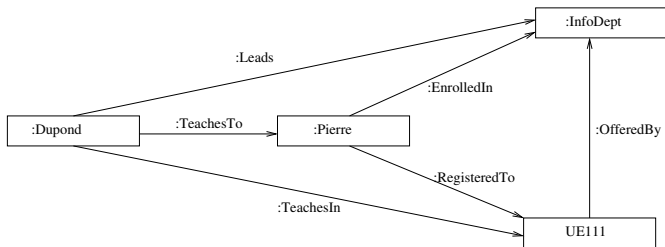
- RDF facts are triplets

```
< :Dupond :Leads :CSDept >  
< :Dupond :TeachesIn :UE111 >  
< :Dupond :TeachesTo :Pierre >  
< :Pierre :EnrolledIn :CSDept >  
< :Pierre :RegisteredTo :UE111 >  
< :UE111 :OfferedBy :CSDept >
```

- Linked open data: publish open data sets on the Web
 - ▶ By September 2011, 31 billions RDF triplets

RDF graph

- A set of RDF facts defines
 - ▶ a set of relations between objects
 - ▶ an **RDF graph** where the nodes are objects:



RDF semantics

- A triplet $\langle s \ P \ o \rangle$ is interpreted in first-order logic (FOL) as a fact $P(s, o)$
- Example:

```
Leads(Dupond, CSDept)
TeachesIn(Dupond, UE111)
TeachesTo(Dupond, Pierre)
EnrolledIn(Pierre, CSDept)
RegisteredTo(Pierre, UE111)
OfferedBy(UE111, CSDept)
```

RDFS: RDF Schema

- Not detailed here: the schema in RDF is super simplistic
- An **RDF Schema** defines the schema of a richer ontology

RDF Schema

- Do not get confused: RDFS can use RDF as syntax, i.e., RDFS statements can be themselves expressed as RDF triplets using some specific **properties** and **objects** used as RDFS keywords with a particular meaning.
- Declaration of classes and subclass relationships
 - ▶ `< Staff rdf:type rdfs:Class >`
 - ▶ `< Java rdfs:subClassOf CSCourse >`
- Declaration of instances (beyond the pure schema)
 - ▶ `< Dupond rdf:type AcademicStaff >`

RDF Schema - continued

- Declaration of relations (properties in RDFS terminology)
 - ▶ `< RegisteredTo rdf:type rdfs:Property >`
- Declaration of subproperty relationships
 - ▶ `< LateRegisteredTo rdfs:subPropertyOf RegisteredTo >`
- Declaration of domain and range restrictions for predicates
 - ▶ `< TeachesIn rdfs:domain AcademicStaff >`
 - ▶ `< TeachesIn rdfs:range Course >`
 - ▶ `TeachesIn(AcademicStaff , Course)`

RDFS logical semantics

RDF and RDFS statements	FOL translation	DL notation
$\langle i \text{ rdf:type } C \rangle$	$C(i)$	$i : C$ or $C(i)$
$\langle i P j \rangle$	$P(i, j)$	$i P j$ or $P(i, j)$
$\langle C \text{ rdfs:subClassOf } D \rangle$	$\forall X (C(X) \Rightarrow D(X))$	$C \sqsubseteq D$
$\langle P \text{ rdfs:subPropertyOf } R \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow R(X, Y))$	$P \sqsubseteq R$
$\langle P \text{ rdfs:domain } C \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow C(X))$	$\exists P \sqsubseteq C$
$\langle P \text{ rdfs:range } D \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow D(Y))$	$\exists P^- \sqsubseteq D$

- Ignore for now DL column
- This is just a notation
- We will come back to it to discuss Description logics

OWL: Web Ontology Language

- OWL extends RDFS with the possibility to express additional constraints
- Main OWL constructs
 - ▶ Disjointness between classes
 - ▶ Constraints of functionality and symmetry on predicates
 - ▶ Intentional class definitions
 - ▶ Class union and intersection
- We will see these are all expressible in Description logics

OWL constructs

- Ignore again the DL column
- Disjointness between classes:

OWL notation	FOL translation	DL notation
$\langle C \text{ owl:disjointWith } D \rangle$	$\forall X (C(X) \Rightarrow \neg D(X))$	$C \sqsubseteq \neg D$

- Constraints of functionality and symmetry on predicates:

OWL notation	FOL translation	DL notation
$\langle \text{P} \text{ rdf:type owl:FunctionalProperty} \rangle$	$\forall X \forall Y \forall Z$ $(P(X, Y) \wedge P(X, Z) \Rightarrow Y = Z)$	$(\text{funct } P)$ or $\exists P \sqsubseteq (\leq 1 P)$
$\langle \text{P} \text{ rdf:type owl:InverseFunctionalProperty} \rangle$	$\forall X \forall Y \forall Z$ $(P(X, Y) \wedge P(Z, Y) \Rightarrow X = Z)$	$(\text{funct } P^-)$ or $\exists P^- \sqsubseteq (\leq 1 P^-)$
$\langle \text{P} \text{ owl:inverseOf } Q \rangle$	$\forall X \forall Y (P(X, Y) \Leftrightarrow Q(Y, X))$	$P \equiv Q^-$
$\langle \text{P} \text{ rdf:type owl:SymmetricProperty} \rangle$	$\forall X \forall Y (P(X, Y) \Rightarrow P(Y, X))$	$P \sqsubseteq P^-$

Definition of intentional classes in OWL

- Goal: allow expressing complex constraints such as:
 - ▶ departments can be lead only by professors
 - ▶ only professors or lecturers may teach to undergraduate students.
- The keyword `owl:Restriction` is used in association with a **blank node class**, and some specific restriction properties:
 - ▶ `owl:someValuesFrom`
 - ▶ `owl:allValuesFrom`
 - ▶ `owl:minCardinality`
 - ▶ `owl:maxCardinality`

OWL Semantics

OWL notation	FOL translation	DL notation
<code>_a owl:onProperty P</code> <code>_a owl:allValuesFrom C</code>	$\forall Y (P(X, Y) \Rightarrow C(Y))$	$\forall P.C$
<code>_a owl:onProperty P</code> <code>_a owl:someValuesFrom C</code>	$\exists Y (P(X, Y) \wedge C(Y))$	$\exists P.C$
<code>_a owl:onProperty P</code> <code>_a owl:minCardinality n</code>	$\exists Y_1 \dots \exists Y_n (P(X, Y_1) \wedge \dots \wedge P(X, Y_n) \wedge \bigwedge_{i,j \in [1..n], i \neq j} (Y_i \neq Y_j))$	$(\geq nP)$
<code>_a owl:maxCardinality n</code>	$\forall Y_1 \dots \forall Y_n \forall Y_{n+1} (P(X, Y_1) \wedge \dots \wedge P(X, Y_n) \wedge P(X, Y_{n+1}) \Rightarrow \bigvee_{i,j \in [1..n+1], i \neq j} (Y_i = Y_j))$	$(\leq nP)$

Unnamed new classes by example

- Departments can be lead only by professors

- Define the set of objects that are lead by professors

```
_a  rdfs:subClassOf    owl:Restriction
_a  owl:onProperty    Leads
_a  owl:allValuesFrom Professor
```

- Now specify that all departments are lead by professors

```
Department  rdfs:subClassOf  _a
```

Union and Intersection of Classes by example

- only professors or lecturers may teach to undergraduate students

```

_a  rdfs:subClassOf      owl:Restriction
_a  owl:onProperty      TeachesTo
_a  owl:someValuesFrom  Undergrad
_b  owl:unionOf         (Professor, Lecturer)
_a  rdfs:subClassOf      _b

```

- This corresponds to an inclusion axiom in Description Logic:

$$\exists \text{TeachesTo. UndergraduateStudent} \sqsubseteq \text{Professor} \sqcup \text{Lecturer}$$

- `owl:equivalentClass` corresponds to double inclusion:

$$\text{MathStudent} \equiv \text{Student} \sqcap \exists \text{RegisteredTo. MathCourse}$$

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 - \mathcal{ALC}
 - Polynomial DLs
- 4 Querying Data through Ontologies
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Description Logics

- Philosophy: isolate **decidable** fragments of first-order logic allowing reasoning on complex logical axioms over unary and binary predicates
- These fragments are called **Description Logics**
- The DL jargon:
 - ▶ the classes are called **concepts**
 - ▶ the properties are called **roles**.
 - ▶ the ontology (the **knowledge base**) = Tbox + Abox
 - ▶ the schema is called the **Tbox**
 - ▶ the instance is called the **Abox**

The DL family

- Few constructs: atomic concepts and roles, inverse of roles, unqualified restriction on roles, restricted negation
- Revisit RDFS checking out the DL column
- If you don't like the syntax: **neither do I**

Semantics of main constructs

- $I(C_1 \sqcap C_2) = I(C_1) \cap I(C_2)$
- $I(\forall R.C) = \{o_1 \mid \forall o_2 [(o_1, o_2) \in I(R) \Rightarrow o_2 \in I(C)]\}$
- $I(\exists R.C) = \{o_1 \mid \exists o_2. [(o_1, o_2) \in I(R) \wedge o_2 \in I(C)]\}$
- $I(\neg C) = \Delta^I \setminus I(C)$
- $I(R^-) = \{(o_2, o_1) \mid (o_1, o_2) \in I(R)\}$

Defining a particular description logic

- Define how to construct complex concepts and roles starting from atomic concepts and roles
 - ▶ *Professor* \sqcup *Lecturer* (those who are either professor or lecturer)
- Choose the constraints you want to consider
- The **complexity** of the logic depends on these choices

Reasoning problems studied in DL

- **Satisfiability checking:** Given a DL knowledge base $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$, is \mathcal{K} satisfiable?
- **Subsumption checking:** Given a Tbox \mathcal{T} and two concept expressions C and D , does $\mathcal{T} \models C \sqsubseteq D$?
- **Instance checking:** Given a DL knowledge base $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$, an individual e and a concept expression C , does $\mathcal{K} \models C(e)$?
- **Query answering:** Given a DL knowledge base $\mathcal{K} = \langle \mathcal{T}, \mathcal{A} \rangle$, and a concept expression C , finds the set of individuals e such that $\mathcal{K} \models C(e)$?

Remarks

- For DLs with full negation: instance checking and subsumption checking can be reduced to (un)satisfiability checking
 - ▶ $\mathcal{T} \models C \sqsubseteq D \Leftrightarrow \langle \mathcal{T}, \{(C \sqcap \neg D)(a)\} \rangle$ is unsatisfiable.
 - ▶ $\langle \mathcal{T}, \mathcal{A} \rangle \models C(e) \Leftrightarrow \langle \mathcal{T}, \mathcal{A} \cup \{\neg C(e)\} \rangle$ is unsatisfiable.
- For DLs without negation: instance checking can be reduced to subsumption checking by computing the **most specific concept** satisfied by an individual in the Abox (denoted $msc(\mathcal{A}, e)$)
 - ▶ $\langle \mathcal{T}, \mathcal{A} \rangle \models C(e) \Leftrightarrow \mathcal{T} \models msc(\mathcal{A}, e) \sqsubseteq C$

\mathcal{ALC} : the prototypical DL

- (standard) An \mathcal{ALC} Abox is made of a set of facts of the form $C(a)$ and $R(a, b)$ where a and b are individuals, R is an atomic role and C is a possibly complex concept
- \mathcal{ALC} constructs:
 - ▶ **conjunction** $C_1 \sqcap C_2$,
 - ▶ **existential restriction** $\exists R.C$
 - ★ $\exists Y (R(X, Y) \wedge C(Y))$
 - ▶ **negation** $\neg C$.
- As a result, \mathcal{ALC} also contains de facto:
 - ▶ **disjunctions** $C_1 \sqcup C_2 (\equiv \neg(\neg C_1 \sqcap \neg C_2))$,
 - ▶ **value restrictions** $(\forall R.C \equiv \neg(\exists R.\neg C))$,
 - ▶ $\top (\equiv A \sqcup \neg A)$ and $\perp (\equiv A \sqcap \neg A)$.

ALC - continued

- An ALC Tbox may contain inclusion constraints between concepts and roles

$$\begin{aligned} \textit{MathCourse} &\sqsubseteq \textit{Course} \\ \textit{LateRegisteredTo} &\sqsubseteq \textit{RegisteredTo} \end{aligned}$$

- An ALC Tbox may contain **General Concept Inclusions** (GCIs):
 $\exists \textit{TeachesTo}.\textit{UndergraduateStudent} \sqsubseteq \textit{Professor} \sqcup \textit{Lecturer}$

Tableau method

- Reasoning is based on tableau calculus - a classical method in logic for checking satisfiability
- Extensively used in Description logics for implementing reasoners
- Technique
 - ▶ Get rid of the Tbox by recursively unfolding the concept definitions
 - ▶ Transform the resulting Abox so that negations applies only to atomic concepts
 - ▶ Try to construct a model or raise a contradiction
- We illustrate the technique with a simple example without GCIs
- In general, much more involved

Tableau method

- For satisfiability checking of a DL knowledge base $\langle \mathcal{T}, \mathcal{A} \rangle$
 - ▶ $\mathcal{T} = \{C_1 \equiv A \sqcap B, C_2 \equiv \exists R.A, C_3 \equiv \forall R.B, C_4 \equiv \forall R. \neg C_1\}$
 - ▶ $\mathcal{A} = \{C_2(a), C_3(a), C_4(a)\}$
- Get rid of the Tbox, by recursively **unfolding** the concept definitions:
 - ▶ $\mathcal{A}' = \{(\exists R.A)(a), (\forall R.B)(a), (\forall R. \neg(A \sqcap B))(a)\} \equiv \langle \mathcal{T}, \mathcal{A} \rangle$
- Transform the concepts expressions in \mathcal{A}' into **negation normal form**
 - ▶ $\mathcal{A}'' = \{(\exists R.A)(a), (\forall R.B)(a), (\forall R. (\neg A \sqcup \neg B))(a)\}$
- Apply **tableau rules** to **extend** the resulting Abox until no rule applies anymore:
 - ▶ From an extended Abox which is **complete** (no rule applies) and **clash-free** (no obvious contradiction), a so-called **canonical interpretation** can be built, which is a model of the initial Abox.

Tableau rules for \mathcal{ALC}

- The \sqcap -rule:

Condition: \mathcal{A} contains $(C \sqcap D)(a)$ but not both $C(a)$ and $D(a)$

Action: add $\mathcal{A}' = \mathcal{A} \cup \{C(a), D(a)\}$

- The \sqcup -rule:

Condition: \mathcal{A} contains $(C \sqcup D)(a)$ but neither $C(a)$ nor $D(a)$

Action: add $\mathcal{A}' = \mathcal{A} \cup \{C(a)\}$ and $\mathcal{A}'' = \mathcal{A} \cup \{D(a)\}$

- The \exists -rule:

Condition: \mathcal{A} contains $(\exists R.C)(a)$ but there is no c such that $\{R(a, c), C(c)\} \subseteq \mathcal{A}$

Action: add $\mathcal{A}' = \mathcal{A} \cup \{R(a, b), C(b)\}$ where b is a new individual name

- The \forall -rule:

Condition: \mathcal{A} contains $(\forall R.C)(a)$ and $R(a, b)$ but not $C(b)$

Action: add $\mathcal{A}' = \mathcal{A} \cup \{C(b)\}$

Illustration on the example

- The result of the application of the tableau method to $\mathcal{A}'' = \{(\exists R.A)(a), (\forall R.B)(a), (\forall R.(\neg A \sqcup \neg B))(a)\}$ gives the following Aboxes:
 - ▶ $\mathcal{A}_1'' = \mathcal{A}'' \cup \{R(a,b), A(b), B(b), \neg A(b)\}$
 - ▶ $\mathcal{A}_2'' = \mathcal{A}'' \cup \{R(a,b), A(b), B(b), \neg B(b)\}$
- They both contain a **clash**:
 \mathcal{A}'' (and the equivalent original knowledge base) is **correctly decided unsatisfiable by the algorithm**

Complexity

- The tableau method shows that the satisfiability of \mathcal{ALC} knowledge bases is decidable but with a complexity that may be **exponential** because of the disjunction construct and the associated \sqcup -rule.
- Satisfiability checking in \mathcal{ALC} (and thus also subsumption and instance checking) is in fact **EXPTIME-complete**
- Additional constructs like those in the fragment **OWL DL** of OWL do not change the complexity class of reasoning (which remains EXPTIME-complete)
- **OWL Full** is undecidable

DLs for which reasoning is polynomial

- \mathcal{FL} : **conjunction** $C_1 \sqcap C_2$, **value restrictions** $\forall R.C$ and **unqualified existential restriction** $\exists R$
 - ▶ For Tboxes without GCIs, subsumption checking is polynomial
 - ▶ For Tboxes with (even simple) GCIs, subsumption checking is co-NP complete
- \mathcal{EL} : **conjunctions** $C_1 \sqcap C_2$ and **existential restrictions** $\exists R.C$
 - ▶ Subsumption checking in \mathcal{EL} is polynomial even for general Tboxes.
- \mathcal{FLE} : **conjunction** $C_1 \sqcap C_2$, **value restrictions** $\forall R.C$, and **existential restrictions** $\exists R.C$
 - ▶ Subsumption checking in \mathcal{FLE} is NP-complete
- The DL-LITE family: a good trade-off, specially designed for guaranteeing **query answering through ontologies** to be polynomial in data complexity.

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 - Querying using RDFS
 - Querying using DL-LITE
 - Complexity
- 5 Conclusion

Querying using RDFS

- RDFS statements can be used to infer new triples
- Example
 - ▶ Base fact *ResponsibleOf*(*durand*, *ue111*)
 - ▶ Use the statement $\langle \textit{ResponsibleOf} \text{ rdfs:domain } \textit{Professor} \rangle$
i.e., the logical rule: $\textit{ResponsibleOf}(X, Y) \Rightarrow \textit{Professor}(X)$
 - ▶ With substitution $\{X/\textit{durand}, Y/\textit{ue111}\}$
 - ▶ Infer fact *Professor*(*durand*)
 - ▶ Use the statement $\langle \textit{Professor} \text{ rdfs:subClassOf } \textit{AcademicStaff} \rangle$
i.e., the rule $\textit{Professor}(X) \Rightarrow \textit{AcademicStaff}(X)$
 - ▶ With substitution $\{X/\textit{durand}\}$
 - ▶ Infer fact *AcademicStaff*(*durand*)
 - ▶ etc.

The saturation algorithm

- Keep inferring new facts until a fixpoint is reached
- Note: Only polynomially many facts can be added
- PTIME

Querying using DL-LITE

- Develop as a good compromise between expressive power and reasonable complexity of query answering
- RDFS simpler and very used but limited
- More complex DL: query answering is unfeasible

The DL-LITE family

- Three kinds of axioms: **positive inclusions** (PI), **negative inclusions** (NI) and **functionality** constraints (func)
- Captures the main constraints used in Databases and Software Engineering
- Different variants
 - ▶ $\text{DL-LITE}_{\mathcal{R}}$: no functionality constraints
 - ▶ $\text{DL-LITE}_{\mathcal{F}}$: no role inclusion
 - ▶ $\text{DL-LITE}_{\mathcal{A}}$: no functionality constraints on roles involved in role inclusions

PI: Positive inclusion and incompleteness

- One of the following forms:

DL notation	Corresponding logical rule
$B \sqsubseteq \exists P$	$B(X) \Rightarrow \exists Y P(X, Y)$
$\exists Q \sqsubseteq \exists P$	$Q(X, Y) \Rightarrow \exists Z P(X, Z)$
$B \sqsubseteq \exists P^-$	$B(X) \Rightarrow \exists Y P(Y, X)$
$\exists Q \sqsubseteq \exists P^-$	$Q(X, Y) \Rightarrow \exists Z P(Z, X)$
$P \sqsubseteq Q^-$ or $P^- \sqsubseteq Q$	$P(X, Y) \Rightarrow Q(Y, X)$

where P and Q denote properties and B denotes a class.

DL notation	Corresponding logical rule
$Professor \sqsubseteq \exists TeachesIn$	$Professor(X) \Rightarrow \exists Y TeachesIn(X, Y)$
$Course \sqsubseteq \exists RegisteredIn^-$	$Course(X) \Rightarrow \exists Y RegisteredIn(Y, X)$

- Not **safe**
- From $Professor(durand)$, I know there is some y $TeachesIn(durand, y)$
- Incompleteness: I don't know y
- Saturation may not terminate

Negative inclusion and inconsistencies

- Negative inclusion takes one of the forms:

$$\frac{\text{DL notation}}{B_1 \sqsubseteq \neg B_2}$$

$$\frac{R_1 \sqsubseteq \neg R_2}{}$$

- where B_1 and B_2 are either classes or expressions of the form $\exists P$ or $\exists P^-$ for some property P
- and where R_1 and R_2 are either properties or inverses of properties.

- Students do not teach courses

DL notation	Corresponding logical rule
$Student \sqsubseteq \neg \exists TeachesIn$	$Student(X) \Rightarrow \neg \exists Y TeachesIn(X, Y)$ or equivalently, $\exists Y TeachesIn(X, Y) \Rightarrow \neg Student(X)$

- The knowledge base may be **inconsistent**
- Not possible with RDFS ontologies

Key constraints and more inconsistencies.

- Axioms of the form $(\text{funct } P)$ or $(\text{funct } P^-)$ where P is a property

DL notation	corresponding logical rule
$(\text{funct } P)$	$P(X, Y) \wedge P(X, Z) \Rightarrow Y = Z$
$(\text{funct } P^-)$	$P(Y, X) \wedge P(Z, X) \Rightarrow Y = Z$

- Key constraints also lead to inconsistencies
- Example:
 - ▶ $(\text{funct } \text{ResponsibleOf}^-)$
 - ▶ A course must have a unique professor responsible for it
 - ▶ If we have $\text{ResponsibleOf}(\text{durand}, \text{ue111})$ and $\text{ResponsibleOf}(\text{dupond}, \text{ue111})$
The KB is inconsistent

Query answering: Example

- Abox:

- ▶ $Professor(Jim), HasTutor(John, Mary), TeachesTo(John, Bill)$

- Tbox:

- ▶ $Professor \sqsubseteq \exists TeachesTo$
- ▶ $Student \sqsubseteq \exists HasTutor$
- ▶ $\exists TeachesTo^- \sqsubseteq Student$
- ▶ $\exists HasTutor^- \sqsubseteq Professor$
- ▶ $Professor \sqsubseteq \neg Student$

- Queries: conjunctive queries on concepts and atomic roles

- ▶ $q_0(x) \leftarrow TeachesTo(x, y) \wedge HasTutor(y, z)$

Query answering: Principles of reformulation

- Transform the query into FO queries over the database
- FO queries are used to check for inconsistencies of the KB
- FO queries are used to evaluate the result
- The FO queries can be evaluated using a database engine with query optimization
- Because of incompleteness, not always possible

Query answering by example (no inconsistency)

- Tbox: \mathcal{T}
 - ▶ $Professor \sqsubseteq \exists TeachesTo$
 - ▶ $Student \sqsubseteq \exists HasTutor$
 - ▶ $\exists TeachesTo^- \sqsubseteq Student$
 - ▶ $\exists HasTutor^- \sqsubseteq Professor$
 - ▶ $Professor \sqsubseteq \neg Student$
- Query:
 - ▶ $q_0(x) \leftarrow TeachesTo(x, y) \wedge HasTutor(y, z)$
- Reformulations of q_0 given the the Tbox \mathcal{T} :
 - ▶ $q_1(x) \leftarrow TeachesTo(x, y) \wedge Student(y)$
 - ▶ $q_2(x) \leftarrow TeachesTo(x, y) \wedge TeachesTo(z', y)$
 - ▶ $q_3(x) \leftarrow TeachesTo(x, y')$
 - ▶ $q_4(x) \leftarrow Professor(x)$
 - ▶ $q_5(x) \leftarrow HasTutor(u, x)$
- **Main result (holds for DL-LITE_A but not for full DL-LITE):**
 - ▶ For any Abox \mathcal{A} such that $\mathcal{T} \cup \mathcal{A}$ is satisfiable:
 $Answer(q_0, \mathcal{T} \cup \mathcal{A}) = \bigcup_i Answer(q_i, \mathcal{A})$

Illustration

- $q_0(x) \leftarrow \textit{TeachesTo}(x, y) \wedge \textit{HasTutor}(y, z)$
- $\textit{Student} \sqsubseteq \exists \textit{HasTutor}$
- $\textit{HasTutor}(y, z) \leftarrow \textit{Student}(y)$
- $q_1(x) \leftarrow \textit{TeachesTo}(x, y) \wedge \textit{Student}(y)$

Example (ctd)

- Abox: \mathcal{A}
 - ▶ *Professor*(Jim), *HasTutor*(John, Mary), *TeachesTo*(John, Bill)
- Query
 - ▶ $q_0(x) \leftarrow \textit{TeachesTo}(x, y) \wedge \textit{HasTutor}(y, z)$
- Reformulations of q_0 given the the Tbox \mathcal{T} :
 - ▶ $q_1(x) \leftarrow \textit{TeachesTo}(x, y) \wedge \textit{Student}(y)$
 - ▶ $q_2(x) \leftarrow \textit{TeachesTo}(x, y) \wedge \textit{TeachesTo}(z', y)$
 - ▶ $q_3(x) \leftarrow \textit{TeachesTo}(x, y')$
 - ▶ $q_4(x) \leftarrow \textit{Professor}(x)$
 - ▶ $q_5(x) \leftarrow \textit{HasTutor}(u, x)$
- Result of the evaluation of the reformulations over \mathcal{A} :
 - ▶ $\text{Answer}(q_0, \mathcal{T} \cup \mathcal{A}) = \{\textit{Mary}, \textit{Jim}, \textit{John}\}$

Consistency checking by example

- Tbox: \mathcal{T}'
 - ▶ $Professor \sqsubseteq \exists TeachesTo$
 - ▶ $Student \sqsubseteq \exists HasTutor$
 - ▶ $\exists TeachesTo^- \sqsubseteq Student$
 - ▶ $\exists HasTutor^- \sqsubseteq Professor$
 - ▶ $Professor \sqsubseteq \neg Student$
 - ▶ $\exists TeachesTo \sqsubseteq \neg Student$
 - ▶ $\exists HasTutor \sqsubseteq Student$
- Saturation of the NIs (possibly using the PIs):
 - ▶ $\exists TeachesTo \sqsubseteq \neg \exists HasTutor$
- Translation of each NI into a boolean conjunctive query:
 - ▶ $q_{unsat} \leftarrow TeachesTo(x, y) \wedge HasTutor(x, y')$
- Evaluation of q_{unsat} on the Abox \mathcal{A} :
 - ▶ $\{Professor(Jim), HasTutor(John, Mary), TeachesTo(John, Bill)\}$
 - ▶ $Answer(q_{unsat}, \mathcal{A}) = \text{true}$
- **Main result:**
 - ▶ $\mathcal{T}' \cup \mathcal{A}$ is inconsistent iff there exists a q_{unsat} such that $Answer(q_{unsat}, \mathcal{A}) = \text{true}$

- Closure of a Tbox: derive new statements
- From $\exists \textit{TeachesTo} \sqsubseteq \neg \textit{Student}$
- Derive $\textit{Student} \sqsubseteq \neg \exists \textit{TeachesTo}$
- From $\exists \textit{HasTutor} \sqsubseteq \textit{Student}$ and $\textit{Student} \sqsubseteq \neg \exists \textit{TeachesTo}$
- Derive $\exists \textit{HasTutor} \sqsubseteq \neg \exists \textit{TeachesTo}$
- From $\exists \textit{HasTutor} \sqsubseteq \neg \exists \textit{TeachesTo}$
- Derive $\exists \textit{TeachesTo} \sqsubseteq \neg \exists \textit{HasTutor}$

FOL reducibility of data management in DL-LITE

Query answering and data consistency checking can be performed in two separate steps:

- 1 A reasoning step with the Tbox alone (i.e., the ontology without the data) and some conjunctive queries
- 2 An evaluation step of conjunctive queries over the data in the Abox (without the Tbox)
 - ▶ makes it possible to use an SQL engine
 - ▶ thus taking advantage of well-established query optimization strategies supported by standard relational DBMS

Complexity results

- The **reasoning step** on Tbox is **polynomial** in the size of the Tbox
 - ▶ Produces a polynomial number of reformulations and of *unsat* queries
- The **evaluation step** over the Abox has the **same data complexity as standard evaluation of conjunctive queries over relational databases**
 - ▶ in AC_0 (strictly contained in *LogSpace* and thus in P)
- The interaction between role inclusion constraints and functionality constraints makes reasoning in DL-LITE **P -complete in data complexity**
 - ▶ full DL-LITE is **not FOL-reducible**
 - ▶ Reformulating a query may require recursion

Problem with full DL-LITE by example

- Let the Tbox (R and P are two properties and S is a class):

$$R \sqsubseteq P$$

$$(\text{funct } P)$$

$$S \sqsubseteq \exists R$$

$$\exists R^- \sqsubseteq \exists R$$

- and the query: $q(x) :- R(z, x)$
- $r_1(x) :- S(x_1), P(x_1, x)$ is a reformulation of the query q given the Tbox
 - from $S(x_1)$ and the PI $S \sqsubseteq \exists R$, it can be inferred: $\exists y R(x_1, y)$, and thus $\exists y P(x_1, y)$ (since $R \sqsubseteq P$).
 - from the functionality constraint on P and $P(x_1, x)$, it can be inferred: $y = x$, and thus: $R(x_1, x)$
 - Therefore: $\exists x_1 S(x_1) \wedge P(x_1, x) \models \exists z R(z, x)$ (i.e., $r_1(x)$ is contained in the query $q(x)$)

Problem with full DL-LITE by example - continued

- r_1 is not the only one reformulation of the query
- In fact, there exists an *infinite* number of different reformulations for $q(x)$:
- for $k \geq 2$, $r_k(x) \text{ :- } S(x_k), P(x_k, x_{k-1}), \dots, P(x_1, x)$ is also a reformulation:
 - ▶ from $S(x_k)$ and the PI $S \sqsubseteq \exists R$, it can be inferred: $\exists y_k R(x_k, y_k)$, and thus $\exists y_k P(x_k, y_k)$ (since $R \sqsubseteq P$).
 - ▶ from the functionality constraint on P and $P(x_k, x_{k-1})$, it can be inferred: $y_k = x_{k-1}$, and thus: $R(x_k, x_{k-1})$
 - ▶ Now, based on the PI $\exists R^- \sqsubseteq \exists R$: $\exists y_{k-1} R(x_{k-1}, y_{k-1})$,
 - ▶ and with the same reasoning as before, we get $y_{k-1} = x_{k-2}$, and thus: $R(x_{k-1}, x_{k-2})$.
 - ▶ By induction, it can be inferred: $R(x_1, x)$, and therefore $r_k(x)$ is contained in the query $q(x)$.

Problem with full DL-LITE by example - end

- One can show that for each k , there exists an Abox such that the reformulation r_k returns answers that are not returned by the reformulation $r_{k'}$ for $k' < k$.
- Thus, there exists an infinite number of *non redundant* conjunctive reformulations.

Outline

- 1 Introduction
- 2 3 ontology languages for the Web
- 3 Reasoning in Description Logics
- 4 Querying Data through Ontologies
- 5 Conclusion**

Conclusion

- The scalability of reasoning on Web data requires **light-weight ontologies**
- One can use a description logic for which reasoning is feasible (polynomial)
- For Aboxes stored as relational databases, it is even preferable that query answering can be performed with a relational query (using query reformulation)
- Full OWL is too complex
- Consider extensions of RDFS